

ELECTRICAL DIPOLE AND QUADRUPOLE TRANSITIONS IN EVEN-EVEN NUCLEI WITH QUADRUPOLE AND OCTUPOLE DEFORMATIONS

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Simple analytical expressions for the reduced probabilities of $E1$ - and $E2$ -transitions of deformable even-even nuclei with quadrupole and octupole deformations are obtained. The ratios of the reduced probabilities of $E1$ - and $E2$ -transitions for ^{104}Ru , ^{166}Er , ^{226}Ra , ^{238}U nuclei are calculated, and they are in satisfactory agreement with experimental data even for high spin-states.

1. Wave Functions

The wave function of axisymmetric even-even nuclei with quadrupole and octupole deformations satisfies the Schrödinger equation [15]

$$\begin{aligned}
 & - \sum_{\lambda=2,3} \frac{\hbar^2}{2B_\lambda} \frac{1}{\beta_\lambda^2} \frac{\partial}{\partial \beta_\lambda} \left(\beta_\lambda^2 \frac{\partial \Psi_I^\pm(\beta_\lambda, \theta)}{\partial \beta_\lambda} \right) + \\
 & + \frac{\hbar^2 I(I+1) \Psi_I^\pm(\beta_\lambda, \theta)}{6(B_2 \beta_2^2 + B_3 \beta_3^2)} + \\
 & + V(\beta_2, \beta_3) \Psi_I^\pm(\beta_\lambda, \theta) = E_I \Psi_I^\pm(\beta_\lambda, \theta), \quad (1)
 \end{aligned}$$

where B_λ are mass parameters, I — spin of the even-even nucleus, $V(\beta_2, \beta_3)$ — potential energy [14], and $\theta = \{\theta_1, \theta_2, \theta_3\}$ — Euler's angles, and looks like

$$\Psi_I^\pm(\beta_2, \beta_3, \theta) = (\beta_2 \beta_3)^{-1} F_I^\pm(\sigma) \chi_\nu(\varepsilon \mp \varepsilon_0) |IM0, \pm\rangle. \quad (2)$$

Here, the function $|IM0, \pm\rangle$ describes rotations of an axisymmetric even-even nucleus with a projection of spin M on the Z , axis and $K = 0$, σ and ε are polar coordinates [10] which change in a region, where $0 \leq \sigma < \infty$, $-\frac{\pi}{2} \leq \varepsilon \leq \frac{\pi}{2}$,

$$\chi_\nu(\xi^\pm) = N_\varepsilon H_\nu(\xi^\pm) \exp\left[-\frac{1}{2}(\xi^\pm)^2\right], \quad (3)$$

where $\xi^\pm = \sqrt{B\omega_\varepsilon(\varepsilon \mp \varepsilon_0)}/2$, N_ε is a normalization coefficient, $H_\nu(\xi^\pm)$ — Hermite polynomial, ε_ν — the eigenvalues of the equation [10,11], $\nu=0, 1, 2, \dots$, and

$$F_I^\pm(x) = N_\sigma x^{S_{(I\nu)}^\pm} e^{-\frac{x}{2}} F(-p, 2S_{(I\nu)}^\pm + 1, x), \quad (4)$$

where N_σ is a normalization coefficient, $F(-p, 2S_{(I\nu)}^\pm + 1, x)$ — degenerate hypergeometric function, $p = 0, 1, 2, \dots$. Here, the designations [14] $g = \frac{BV_0\sigma_0^2}{\hbar^2} (S_{(I\nu)}^\pm)^2 = \frac{I(I+1)}{3} + 2g \mp \frac{2B}{\hbar^2} \varepsilon_\nu$, $x = \frac{2\sqrt{-2B(E_I^\pm - V_0)}}{\hbar} \sigma$ are used.

Introduction

Atomic nuclei with quadrupole and octupole deformations have two rotational bands with opposite values of parity [1–5]. Energies of levels of these rotational bands, quadrupole and dipole transitions, magnitude of polarization-related electric dipole moment were studied for isotopes of barium, cerium, thorium, radium, actinium and several other nuclei [1–13]. In these nuclei, besides the main rotational band 0^+ , 2^+ , 4^+ , ..., the band 1^- , 3^- , 5^- , ... with a projection of the spin on the axis of symmetry of a nucleus $K = 0$ was also observed.

The energy spectrum of an axial-symmetric nucleus with quadrupole and octupole deformations is calculated in [14] within the framework of phenomenological non-adiabatic collective theory. The carried out comparison of theoretical calculations of energy of the excited levels with experimental data for ^{162}Dy , ^{226}Ra , ^{232}Th , ^{232}U , ^{236}U , ^{238}U nuclei has shown that the offered model describes these data well, including levels with high spins.

The accounting of deformability of a nucleus, except for a change of the arrangement of energy levels, should affect the reduced probabilities of $E1$ - and $E2$ -transitions between the levels of even and odd bands. Therefore, the description of the reduced probabilities of $E1$ - and $E2$ -transitions from the above-stated bands on the basis of phenomenological non-adiabatic collective theory is actual.

2. Electric Dipole and Quadrupole Transitions

The reduced probabilities of $E2$ -transitions between levels $|pI_i0\rangle$ and $\langle p'I_f0|$ are determined by the expressions

$$B(E2, I_i \rightarrow I_f) = B_a(E2, I_i \rightarrow I_f) S_{I_f I_i}^2(E2) \exp\left(-\hbar/2(BC_\varepsilon)^{1/2}\right), \quad (5)$$

$$B_a(E2, I_i \rightarrow I_f) = \frac{5}{16\pi} Q_0^2 (I_i 200 / I_f 0)^2, \quad (6)$$

where $B_a(E2, I_i \rightarrow I_f)$ is the probability of $E2$ -transition between the excited states of even-even nuclei in the adiabatic approach [16], and Q_0 – the internal quadrupole moment of a nucleus. The multiplier $S_{I_f I_i}$ takes into account the deformability of a nucleus and is determined as

$$S_{I_f I_i} \equiv \langle pI_f0 | \frac{\sigma}{\sigma_0} | p'I_i0 \rangle = \int_0^\infty F_{I_f}^\pm(\sigma) \frac{\sigma}{\sigma_0} F_{I_i}^\pm(\sigma) d\sigma. \quad (7)$$

The general expression for matrix elements (7) is very awkward. Therefore, we consider special cases. Let states $|pI_i0\rangle$ and $\langle p'I_f0|$ belong to the collective excited states of the main ($p = 0$) and the first rotational- β -vibrational bands ($p = 1$) with quadrupole and octupole deformations. Then, it is necessary to take $p=0, 1$ in formula (7).

Thus, assuming $p = 0, 1$ in the states of collective excitation, which are referred to the main and first rotational- β -vibrational bands with quadrupole and octupole deformations in wave function (2), we obtain the following formulas for calculation of the reduced probability of $E2$ -transitions for the even-even nuclei.

$$B(E2, I_i \rightarrow I_f) = \left[\frac{(2s_i + 2)^2}{8g} \sqrt{\frac{1}{\Gamma(2s_f + 2)\Gamma(2s_i + 2)}} \times \left(\frac{2s_i + 2}{2s_f + 2} \right)^{s_f} \left(\frac{2s_f + 1}{s_i + s_f + 1} \right)^{s_i + s_f + 2} \right]^2 \times \Gamma^2(s_i + s_f + 2) B_a(E2, I_i \rightarrow I_f) \exp\left(-\hbar/2(BC_\varepsilon)^{1/2}\right) \quad (8)$$

are the probabilities of $E2$ -transitions inside the main rotational- β -vibrational band with quadrupole and octupole deformations;

$$B(E2, I_i \rightarrow I_f) = \left[\frac{(2s_i + 3)^2}{8g} \sqrt{\frac{2s_i + 1}{(2s_i + 3)\Gamma(2s_i + 1)\Gamma(2s_f + 2)}} \times$$

$$\times \left(\frac{2s_i + 3}{2s_f + 1} \right)^{s_f} \left(\frac{2s_f + 1}{s_i + s_f + 2} \right)^{s_i + s_f + 2} \right]^2 \times \left(1 - \frac{2s_f + 1}{2s_i + 2} \right)^2 \Gamma^2(s_i + s_f + 2) B_a(E2, I_i \rightarrow I_f) \times \exp\left(-\hbar/2(BC_\varepsilon)^{1/2}\right) \quad (9)$$

the probabilities of $E2$ -transitions between the main and first rotational- β -vibrational bands with quadrupole and octupole deformations;

$$B(E2, I_i \rightarrow I_f) = \left[\frac{(2s_i + 3)^2}{8g} \left(\frac{2s_i + 3}{2s_f + 3} \right)^{s_f} \left(\frac{2s_f + 3}{s_i + s_f + 3} \right)^{s_i + s_f + 2} \right]^2 \times \left(1 - \frac{(2s_f + 3)(s_f + 1) + (2s_i + 3)(s_i + 1)}{2(s_i + 1)(s_f + 1)} \right) \times \left(\frac{s_i + s_f + 2}{s_i + s_f + 3} + \frac{(2s_i + 3)(2s_f + 3)(s_i + s_f + 2)}{4(s_i + 1)(s_f + 1)(s_i + s_f + 3)} \right)^2 \times \frac{(2s_i + 1)(2s_f + 1)\Gamma^2(s_i + s_f + 2)}{(2s_i + 3)(2s_f + 3)\Gamma(2s_i + 1)\Gamma(2s_f + 1)} \times B_a(E2, I_i \rightarrow I_f) \exp\left(-\hbar/2(BC_\varepsilon)^{1/2}\right) \quad (10)$$

– the probabilities of $E2$ -transitions inside the first rotational- β -vibrational band with quadrupole and octupole deformations.

The reduced probabilities of electric dipole transitions between the levels $|pI_i0\rangle$ and $\langle p'I_f0|$ with opposite parities are defined as

$$B(E1, I_i \rightarrow I_f) = B_a(E1, I_i \rightarrow I_f) S_{I_f I_i}^2 \exp\left(-\frac{2\hbar}{\sqrt{BC_\varepsilon}}\right), \quad (11)$$

where

$$B_a(E1, I_i \rightarrow I_f) = \frac{3}{4\pi} D_0^2 (I_i 100 / I_f 0)^2 \quad (12)$$

are the probabilities of $E1$ -transitions between excited states of even-even nuclei in the adiabatic approximation [16]. Here, $D_0 = \frac{9AZe^3}{56\pi\sqrt{35}} \left(\frac{1}{J} + \frac{15}{8QA^{1/3}} \right) \beta_2^0 \beta_3^0$ is the polarization-related electric dipole moment [9], and

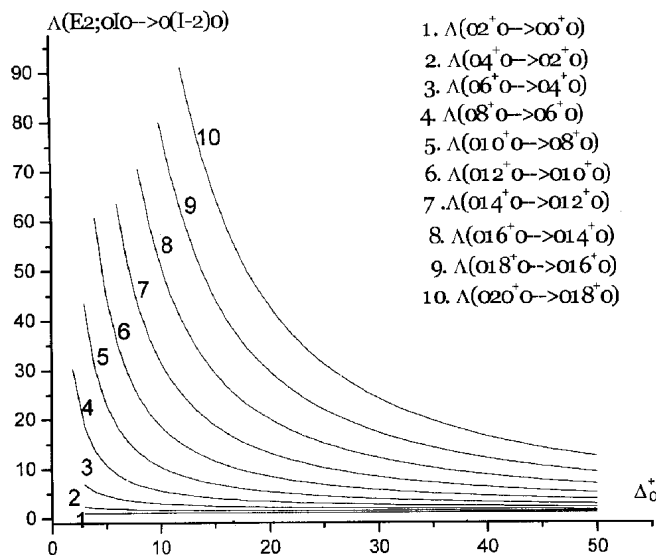


Fig. 1. Dependences of the ratios of the reduced probabilities of $E2$ -transitions between the energy levels of positive parity to the reduced probability of $E2$ -transition from the state of the first excited level with spin 2^+ to the ground state on the parameter Δ_0^+

$S_{I_i I_f}(E1)$ is the factor conditioned by quadrupole and octupole deformations of the nucleus surface,

$$S_{I_i I_f} \equiv \langle p I_f 0 | \frac{\sigma^2}{\sigma_0^2} | p' I_i 0 \rangle = \int_0^\infty F_{I_f}^+(\sigma) \frac{\sigma^2}{\sigma_0^2} F_{I_i}(\sigma) d\sigma. \quad (13)$$

By analyzing partial cases, like the case of $E2$ -transitions, we get the following formulas for the calculation of the reduced probability of electric dipole transitions in even-even nuclei:

$$\begin{aligned} B(E1, I_i \rightarrow I_f) = & \left\{ \frac{(2s_i + 3)^3}{64g^2} \left(\frac{2s_i + 1}{2s_f + 2} \right)^{s_f} \left(\frac{2s_f + 1}{s_i + s_f + 1} \right)^{s_i + s_f + 3} \right. \\ & \left. \times \frac{\Gamma(s_i + s_f + 3)}{\sqrt{\Gamma(2s_f + 2)\Gamma(2s_i + 2)}} \right\}^2 \times \\ & \times B_a(E1, I_i \rightarrow I_f) \exp\left(-\frac{2\hbar}{\sqrt{BC_\epsilon}}\right) \end{aligned} \quad (14)$$

are the probabilities of $E1$ -transitions between the levels of the octupole and main rotational- β -vibrational bands with quadrupole and octupole deformations, where $s_f^2 = \frac{I(I-1)}{3} + \Delta_0^+$ and $s_i^2 = \frac{I(I+1)}{3} + \Delta_0^-$;

$$B(E1, I_i \rightarrow I_f) =$$

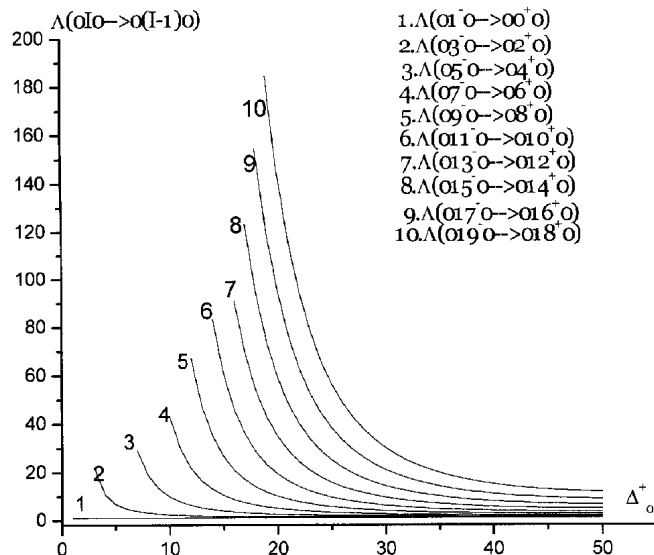


Fig. 2. Dependence of the ratios of the reduced probabilities of $E1$ -transitions between the energy levels of negative and positive parity to the reduced probability of $E1$ -transition from the state of the excited level with spin 1^- to the ground state on the parameter Δ_0^+ at the fixed parameter $\Delta_0^- = 50$

$$\begin{aligned} = & \left\{ \frac{(2s_i + 3)^3}{64g^2} \left(\frac{2s_i + 3}{2s_f + 2} \right)^{s_f} \left(\frac{2s_f + 1}{s_i + s_f + 2} \right)^{s_i + s_f + 3} \right. \\ & \left. \times \frac{\sqrt{2s_i + 1}\Gamma(s_i + s_f + 3)}{\sqrt{(2s_i + 3)\Gamma(2s_i + 1)\Gamma(2s_f + 2)}} \right\}^2 \times \\ & \times \left(1 - \frac{(2s_f + 1)(s_i + s_f + 3)}{(2s_i + 2)(s_i + s_f + 2)} \right) \times \\ & \times B_a(E1, I_i \rightarrow I_f) \exp\left(-\frac{2\hbar}{\sqrt{BC_\epsilon}}\right) \end{aligned} \quad (15)$$

— the probabilities of $E1$ -transitions between the levels of the first rotational- β -vibrational band with quadrupole and octupole deformations, where $s_f^2 = \frac{I(I-1)}{3} + \Delta_0^-$ and $s_i^2 = \frac{I(I+1)}{3} + \Delta_0^+$.

It is convenient to consider the ratios of the reduced probabilities of $E1$ - and $E2$ -transitions to the reduced probability of EL -transitions from the states of the first quadrupole and dipole excitations ($L = 2$ for quadrupole transitions and $L = 1$ for dipole ones) to the ground state:

$$\Lambda(EL, I_i \rightarrow I_f) = \frac{B(EL, I_i \rightarrow I_f)}{B(EL, L \rightarrow 0)}. \quad (16)$$

T a b l e 1. Theoretical and experimental values of the ratios of the reduced probabilities of $E2$ -transitions

| Nucleus and parameters | $E2$ -transitions | Theory | Experiment |
|------------------------|--|--------|---------------------------|
| ^{104}Ru | $02^+0 \rightarrow 00^+0/02^+0 \rightarrow 00^+0$ | 1 | 1 |
| $\Delta_0^+ = 40.0$ | $04^+0 \rightarrow 02^+0/02^+0 \rightarrow 00^+0$ | 1.34 | 1.3(6) |
| $\Delta_0^- = 161.24$ | $06^+0 \rightarrow 04^+0/02^+0 \rightarrow 00^+0$ | 1.72 | 2.2(6) |
| [17] | $08^+0 \rightarrow 06^+0/02^+0 \rightarrow 00^+0$ | 2.28 | 2.2(2) |
| | $010^+0 \rightarrow 08^+0/02^+0 \rightarrow 00^+0$ | 3.14 | 2.1(6) |
| | $05^-0 \rightarrow 03^-0/02^+0 \rightarrow 00^+0$ | 0.80 | 0.79(8) |
| ^{166}Er | $02^+0 \rightarrow 00^+0/02^+0 \rightarrow 00^+0$ | 1 | 1 |
| $\Delta_0^+ = 27.0$ | $04^+0 \rightarrow 02^+0/02^+0 \rightarrow 00^+0$ | 1.4 | 1.4(1) |
| [17] | $06^+0 \rightarrow 04^+0/04^+0 \rightarrow 02^+0$ | 1.37 | 0.9(3) |
| | $010^+0 \rightarrow 08^+0/08^+0 \rightarrow 06^+0$ | 1.49 | 1.2(1) |
| | $010^+0 \rightarrow 08^+0/08^+0 \rightarrow 06^+0$ | 1.49 | 1.1(1) |
| | $012^+0 \rightarrow 010^+0/010^+0 \rightarrow 08^+0$ | 1.51 | 1.0(1) |
| | $012^+0 \rightarrow 010^+0/010^+0 \rightarrow 08^+0$ | 1.51 | 1.9(1) |
| ^{226}Ra | $00^+0 \rightarrow 02^+0/00^+0 \rightarrow 02^+0$ | 1 | $1.000_{-0.009}^{+0.009}$ |
| $\Delta_0^+ = 400.0$ | $02^+0 \rightarrow 04^+0/00^+0 \rightarrow 02^+0$ | 0.437 | $0.874_{-0.009}^{+0.008}$ |
| [16] | $04^+0 \rightarrow 06^+0/00^+0 \rightarrow 02^+0$ | 0.378 | $0.536_{-0.005}^{+0.005}$ |
| | $06^+0 \rightarrow 08^+0/00^+0 \rightarrow 02^+0$ | 0.364 | $0.468_{-0.004}^{+0.004}$ |
| | $08^+0 \rightarrow 010^+0/00^+0 \rightarrow 02^+0$ | 0.366 | $0.507_{-0.005}^{+0.005}$ |
| | $010^+0 \rightarrow 012^+0/00^+0 \rightarrow 02^+0$ | 0.377 | $0.295_{-0.003}^{+0.003}$ |
| | $012^+0 \rightarrow 014^+0/00^+0 \rightarrow 02^+0$ | 0.396 | $0.441_{-0.004}^{+0.004}$ |
| | $014^+0 \rightarrow 016^+0/00^+0 \rightarrow 02^+0$ | 0.421 | $0.388_{-0.004}^{+0.003}$ |
| | $016^+0 \rightarrow 018^+0/00^+0 \rightarrow 02^+0$ | 0.453 | $0.402_{-0.004}^{+0.004}$ |
| | $018^+0 \rightarrow 020^+0/00^+0 \rightarrow 02^+0$ | 0.491 | $0.472_{-0.009}^{+0.005}$ |
| | $020^+0 \rightarrow 022^+0/00^+0 \rightarrow 02^+0$ | 0.536 | $0.755_{-0.008}^{+0.007}$ |
| | $022^+0 \rightarrow 024^+0/00^+0 \rightarrow 02^+0$ | 0.589 | $0.851_{-0.012}^{+0.018}$ |
| | $024^+0 \rightarrow 026^+0/00^+0 \rightarrow 02^+0$ | 0.650 | $0.420_{-0.004}^{+0.006}$ |
| | $026^+0 \rightarrow 028^+0/00^+0 \rightarrow 02^+0$ | 0.720 | $0.682_{-0.041}^{+0.071}$ |
| | $028^+0 \rightarrow 030^+0/00^+0 \rightarrow 02^+0$ | 0.800 | $0.455_{-0.007}^{+0.028}$ |
| | $032^+0 \rightarrow 034^+0/00^+0 \rightarrow 02^+0$ | 0.890 | $0.185_{-0.004}^{+0.005}$ |
| ^{238}U | $00^+0 \rightarrow 02^+0/00^+0 \rightarrow 02^+0$ | 1 | 1 |
| $\Delta_0^+ = 400.0$ | $06^+0 \rightarrow 08^+0/00^+0 \rightarrow 02^+0$ | 0.36 | 0.40(6) |
| [17] | $010^+0 \rightarrow 012^+0/00^+0 \rightarrow 02^+0$ | 0.38 | 0.44(6) |
| | $012^+0 \rightarrow 014^+0/00^+0 \rightarrow 02^+0$ | 0.40 | 0.44(5) |
| | $014^+0 \rightarrow 016^+0/00^+0 \rightarrow 02^+0$ | 0.42 | 0.43(4) |
| | $016^+0 \rightarrow 018^+0/00^+0 \rightarrow 02^+0$ | 0.45 | 0.34(6) |
| | $018^+0 \rightarrow 020^+0/00^+0 \rightarrow 02^+0$ | 0.49 | 0.38(6) |
| | $020^+0 \rightarrow 022^+0/00^+0 \rightarrow 02^+0$ | 0.54 | 0.33(6) |
| | $022^+0 \rightarrow 024^+0/00^+0 \rightarrow 02^+0$ | 0.59 | 0.44(4) |
| | $024^+0 \rightarrow 026^+0/00^+0 \rightarrow 02^+0$ | 0.65 | 0.48(2) |
| | $026^+0 \rightarrow 028^+0/00^+0 \rightarrow 02^+0$ | 0.72 | 0.44(2) |

The ratio of the reduced probabilities of $E2$ -transitions between the energy levels of the same parity is determined by the parameter Δ_0^+ for the even band and by Δ_0^- for the odd band. But the ratio of the reduced probabilities of $E1$ -transitions between the energy levels of different parities is determined by the parameters Δ_0^+ and Δ_0^- .

In Figs. 1, 2, the ratios of reduced probabilities of $E1$ - and $E2$ -transitions vs the parameter Δ_0^+ are shown. For $E1$ -transitions, we fix $\Delta_0^- = 50$.

T a b l e 2. Theoretical and experimental values of the ratios of reduced probabilities of $E1$ -transitions

| Nucleus and parameters | $E1$ -transitions | Theory | Experiment |
|------------------------|---|--------|---------------------------|
| ^{226}Ra | $00^+0 \rightarrow 01^-0/00^+0 \rightarrow 01^-0$ | 1.000 | $1.000_{-0.392}^{+0.392}$ |
| $\Delta_0^+ = 200.0$ | $02^+0 \rightarrow 03^-0/00^+0 \rightarrow 01^-0$ | 0.546 | $0.617_{-0.235}^{+0.235}$ |
| $\Delta_0^- = 190.$ | $04^+0 \rightarrow 05^-0/00^+0 \rightarrow 01^-0$ | 0.526 | $0.298_{-0.111}^{+0.111}$ |
| [16] | $06^+0 \rightarrow 07^-0/00^+0 \rightarrow 01^-0$ | 0.558 | $0.186_{-0.068}^{+0.068}$ |
| | $08^+0 \rightarrow 09^-0/00^+0 \rightarrow 01^-0$ | 0.624 | $0.384_{-0.141}^{+0.141}$ |
| | $012^+0 \rightarrow 013^-0/00^+0 \rightarrow 01^-0$ | 0.863 | $0.758_{-0.276}^{+0.276}$ |
| | $014^+0 \rightarrow 015^-0/00^+0 \rightarrow 01^-0$ | 1.051 | $1.176_{-0.594}^{+0.594}$ |
| | $016^+0 \rightarrow 017^-0/00^+0 \rightarrow 01^-0$ | 1.302 | $1.355_{-0.497}^{+0.497}$ |
| | $018^+0 \rightarrow 019^-0/00^+0 \rightarrow 01^-0$ | 1.630 | $1.535_{-0.605}^{+0.605}$ |
| | $020^+0 \rightarrow 021^-0/00^+0 \rightarrow 01^-0$ | 2.056 | $2.074_{-0.777}^{+0.777}$ |
| | $022^+0 \rightarrow 023^-0/00^+0 \rightarrow 01^-0$ | 2.606 | $2.130_{-0.878}^{+0.878}$ |
| | $024^+0 \rightarrow 025^-0/00^+0 \rightarrow 01^-0$ | 3.308 | $6.350_{-2.389}^{+2.389}$ |
| | $026^+0 \rightarrow 027^-0/00^+0 \rightarrow 01^-0$ | 4.206 | $6.259_{-2.290}^{+2.587}$ |
| | $030^+0 \rightarrow 031^-0/00^+0 \rightarrow 01^-0$ | 6.760 | $3.903_{-1.658}^{+1.468}$ |

It is seen from Figs. 1, 2 that the ratios of the reduced probabilities of $E1$ - and $E2$ -transitions decrease with different rates with increase in parameter Δ_0^+ . At a fixed value of the parameter Δ_0^+ , the ratios of the reduced probabilities of these transitions increase with the spin of levels of a nucleus.

In Tables 1, 2, the comparison of theoretical and experimental values of the ratios of reduced probabilities of $E2$ - and $E1$ -transitions is carried out for ^{104}Ru , ^{166}Er , ^{226}Ra , and ^{238}U nuclei at several values of the parameters Δ_0^+ and Δ_0^- . It is seen from Tab. 1, 2, that the given theory describes the ratios of the reduced probabilities satisfactorily.

Conclusion

Thus, a simple consideration of the reduced probabilities of $E1$ - and $E2$ -transitions of the even-even nuclei with quadrupole and octupole deformations with regard for a change of the shape of a nucleus at the excitation is offered in the present paper, and analytical expressions for these quantities are obtained. The ratios of the reduced probabilities of $E1$ - and $E2$ -transitions are determined by two parameters Δ_ν^+ and Δ_ν^- and are different for even and odd bands. For all the nuclei, we have $\Delta_\nu^+ < \Delta_\nu^-$, which is connected to the presence of a tunnel transition between the shapes of the nuclei with opposite values of the octupole deformation.

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ЕЛЕКТРИЧНІ ДИПОЛЬНІ І КВАДРУПОЛЬНІ ПЕРЕХОДИ
В ПАРНО-ПАРНИХ ЯДРАХ З КВАДРУПОЛЬНОЮ
І ОКТУПОЛЬНОЮ ДЕФОРМАЦІЯМИ

Ш. Шаріпов, М.С. Надирбеков

Резюме

Отримано прості аналітичні вирази для зведених імовірностей $E1$ - та $E2$ -переходів у деформованих парно-парних ядрах з квадрупольною і октупольною деформаціями. Обчислено значення вказаних імовірностей для ядер ^{104}Ru , ^{166}Er , ^{226}Ra , ^{238}U . Результати обчислень задовільно узгоджуються з експериментальними даними, в тому числі для станів з великими спінами.